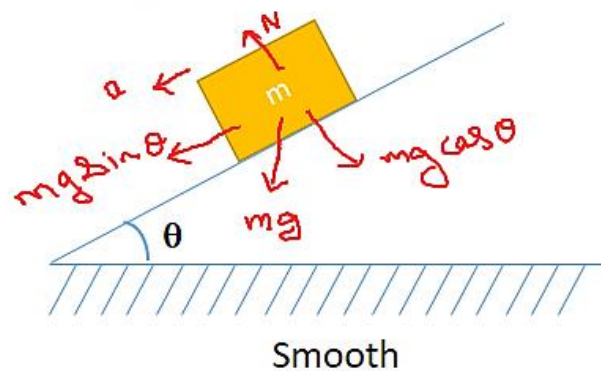




In the figure shown, find acceleration of the block and contact force acting on the block.

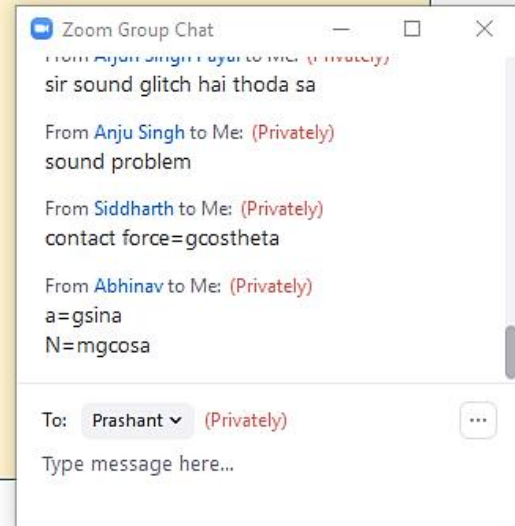


$$a = g \sin \theta$$

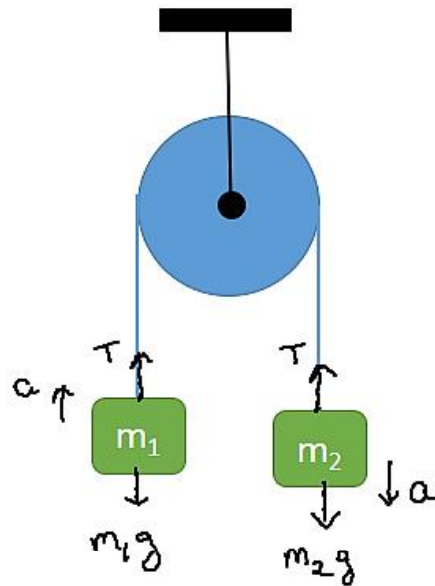
$$N = mg \cos \theta$$

$$a = \frac{mg \sin \theta}{m} = g \sin \theta$$

$$N = mg \cos \theta$$



# ATWOOD MACHINE



$$a = \left( \frac{m_2 - m_1}{m_2 + m_1} \right) g$$

$$T = \left( \frac{2m_1m_2}{m_2 + m_1} \right) g$$

$$\begin{aligned}
 m_2g - \cancel{T} &= m_2a & \text{--- (1)} \\
 \cancel{T} - m_1g &= m_1a & \text{--- (2)} \\
 \hline
 (m_2 - m_1)g &= (m_2 + m_1)a \\
 a &= \frac{(m_2 - m_1)g}{m_2 + m_1} \\
 T &= m_1 \left( \frac{m_2 - m_1}{m_2 + m_1} \right) g + m_1g \\
 &= \frac{2m_1m_2g}{m_1 + m_2}
 \end{aligned}$$

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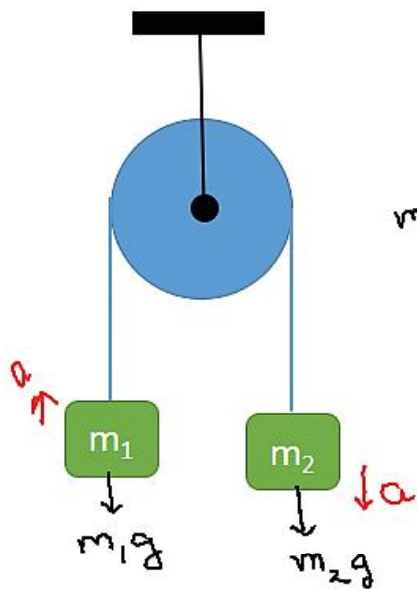
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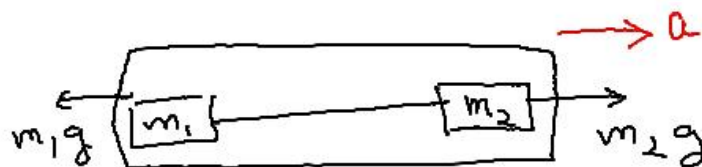
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# ATWOOD MACHINE



$$a = \left( \frac{m_2 - m_1}{m_2 + m_1} \right) g$$

$$T = \left( \frac{2m_1m_2}{m_2 + m_1} \right) g$$



$$m_2g - m_1g = (m_2 + m_1)a$$

$$a = \frac{(m_2 - m_1)g}{m_2 + m_1}$$

Physics by Ritesh Agarwal (B. Tech. IIT Bombay)

Zoom Group Chat

From Karamchand Prasad to Me: (Privately)  
yes

From Aryan Dhiman to Me: (Privately)  
SIR ASSIGNMENT KA EK QUESTION  
GALAT HAI KAL WALI ASSIGNMENT ME

From Mansi Kansal to Me: (Privately)  
 $m_2 - m_1 / m_1 + m_2 \times g$

From Aditi Rai to Me: (Privately)  
 $m_2g / m_1$  plus 2 is acc

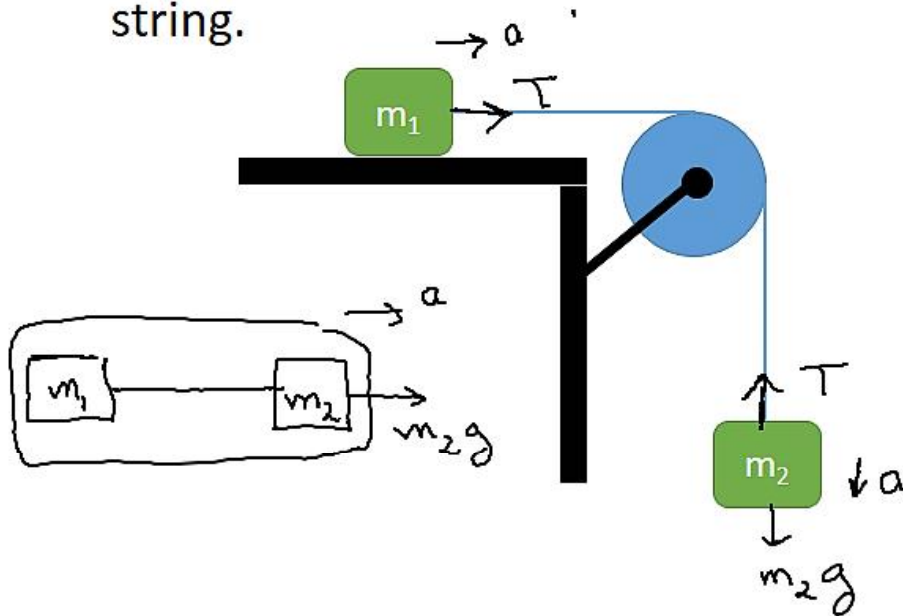
To: Prashant (Privately)

Type message here...



## Example

Find acceleration of blocks and tension in the string.



$$a = \frac{m_2g}{m_1 + m_2} \quad T = \frac{m_1m_2g}{m_1 + m_2}$$

Physics by Ritesh Agarwal (B. Tech. IIT Bombay)

$$m_2g = (m_2 + m_1)a$$

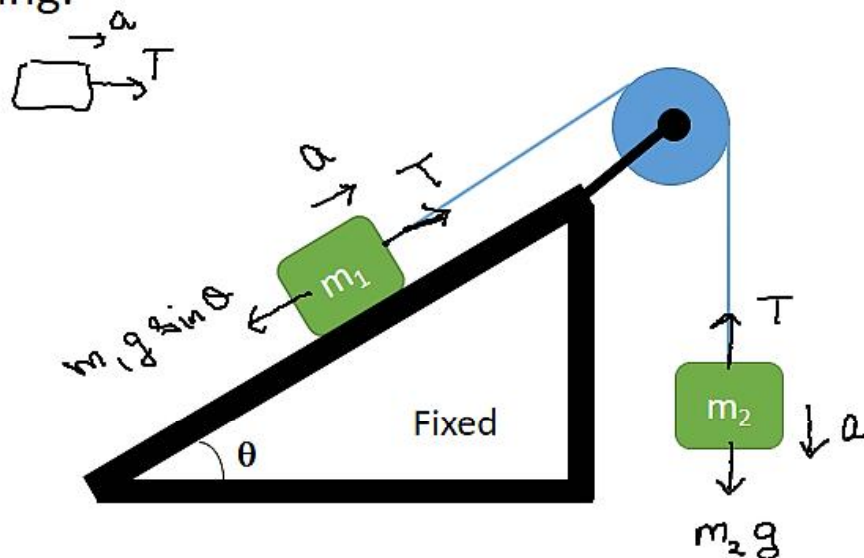
$$a = \frac{m_2g}{m_1 + m_2}$$

$$T = m_1a$$

$$= \frac{m_1m_2g}{m_1 + m_2}$$

## Example

Find acceleration of blocks and tension in the string.



$$a = \frac{(m_2 - m_1 \sin \theta)g}{m_1 + m_2} \quad T = \frac{m_1 m_2 g (1 + \sin \theta)}{m_1 + m_2}$$

Physics by Ritesh Agarwal (B. Tech. IIT Bombay)

$$m_2 g - m_1 g \sin \theta = (m_2 + m_1) a$$

$$a = \frac{(m_2 - m_1 \sin \theta) g}{m_2 + m_1}$$

$$m_2 g - T = m_2 a$$

$$T = m_2 g - m_2 a$$

$$= m_2 g - \frac{m_2 (m_2 - m_1 \sin \theta) g}{m_2 + m_1}$$

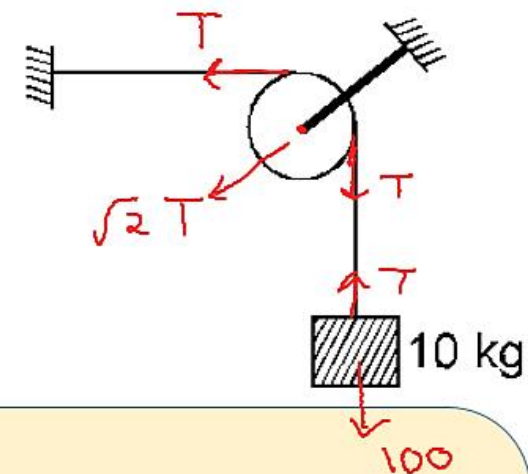
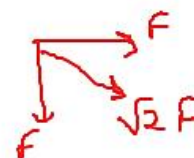
$$= \frac{\cancel{m_2^2} g + m_1 m_2 g - \cancel{m_2^2} g + m_1 m_2 g \sin \theta}{m_2 + m_1}$$

$$= \frac{m_1 m_2 g (1 + \sin \theta)}{m_1 + m_2}$$



## Example

Find magnitude of force exerted by string on pulley.



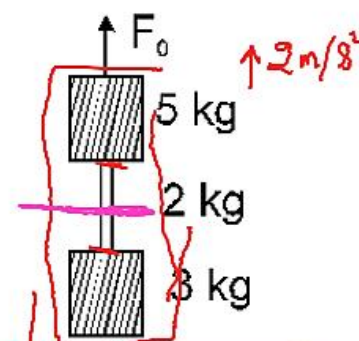
$$T = 100\text{ N}$$

$$\sqrt{2}T = 100\sqrt{2} = 141\text{ N}$$

## Example

A 5 kg block has a rope of mass 2 kg attached to its underside and a 3 kg block is suspended from the other end of the rope. The whole system is accelerated upward at  $2 \text{ m/s}^2$  by an external force  $F_0$ .

- What is  $F_0$ ?
- What is the net force on rope? ✓
- What is the tension at middle point of the rope? ( $g = 10 \text{ m/s}^2$ ) ✓

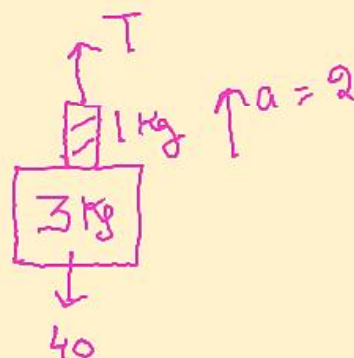


$$F_0 - 100 = 10 \times 2 \Rightarrow F_0 = 120 \text{ N} \checkmark$$

$$F_{\text{net}} = ma = 2 \times 2 = 4 \text{ N} \checkmark$$

$$T - 40 = 4 \times 2$$

$$T = 48 \text{ N}$$



# SPRING FORCE

The extension or compression produced in a spring is directly proportional to the force applied on it.

If  $x$  is the deformation in the spring then

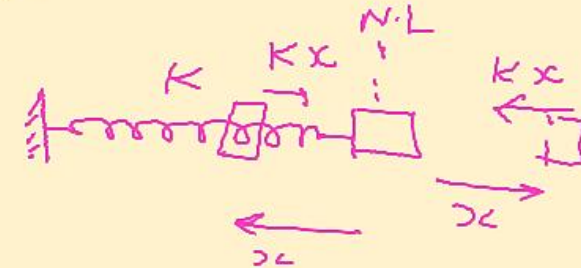
$$F \propto x$$

or

$$F = -kx$$

where  $k$  is constant and is called the spring constant or force constant.

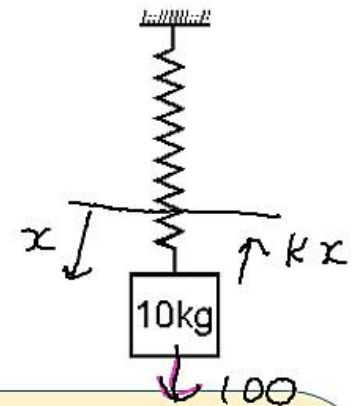
The negative sign shows that the force and the extension or compression are opposite in their directions.





## Example

Force constant of a spring is 100 N/m. If a 10 kg block attached with the spring is at rest, then find extension in the spring. ( $g = 10 \text{ m/s}^2$ )



$$Kx = 100$$

$$x = \frac{100}{K} = 1 \text{ m}$$

# PSEUDO FORCE

Hypothetical force used to apply law's of motion in accelerated (non-inertial) frames.

$$\vec{F}_{\text{Pseudo}} = \ominus m \vec{a}_{\text{Frame}}$$

↑  
object

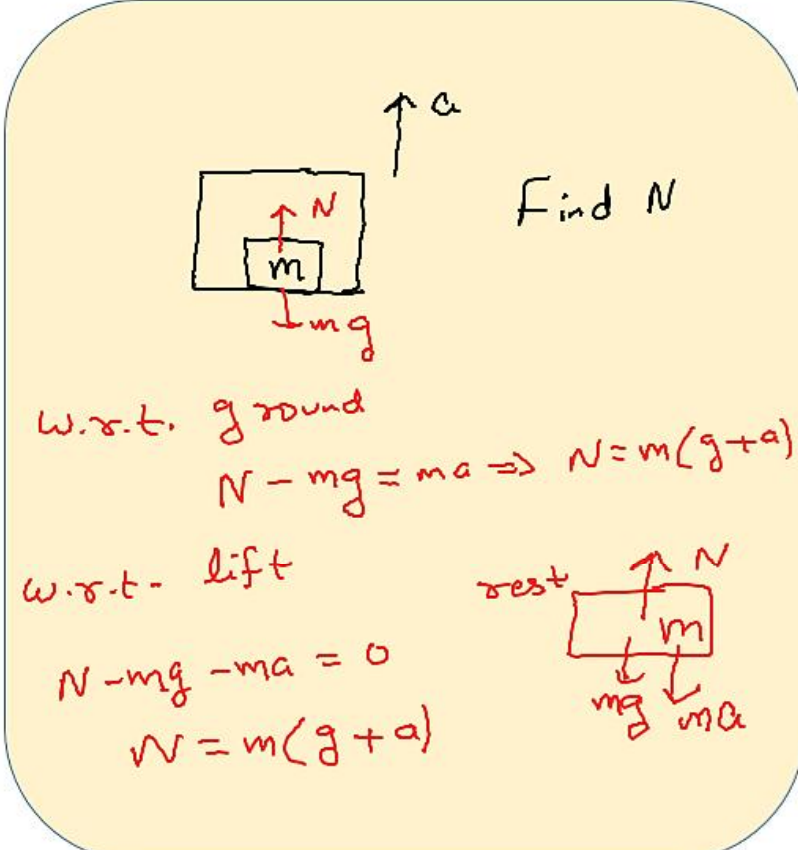


Diagram showing a block of mass  $m$  inside a lift accelerating upwards with acceleration  $a$ . Forces acting on the block are Normal force  $N$  (up) and weight  $mg$  (down). The text "Find  $N$ " is written next to the diagram.

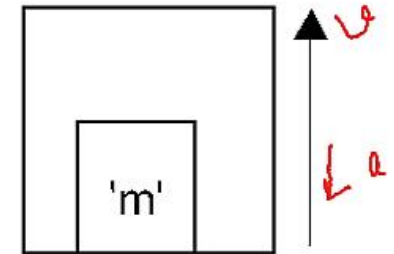
w.r.t. ground  
 $N - mg = ma \Rightarrow N = m(g + a)$

w.r.t. lift  
 $N - mg - ma = 0$   
 $N = m(g + a)$

rest frame diagram: A block of mass  $m$  with forces  $N$  (up),  $mg$  (down), and  $ma$  (down) shown.

## Example

A box is moving upward with retardation ' $a$ '  $< g$ , find the direction and magnitude of "pseudo force" acting on block of mass ' $m$ ' placed inside the box. Also calculate normal force exerted by surface on block



Wrt lift

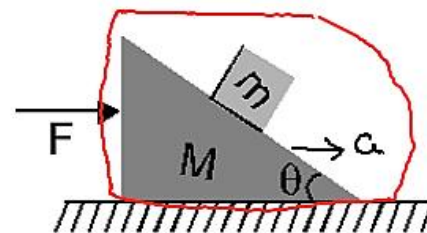


$$N + ma - mg = 0$$

$$N = m(g - a)$$

## Example

All surfaces are smooth in the adjoining figure. Find F such that block remains stationary with respect to wedge.



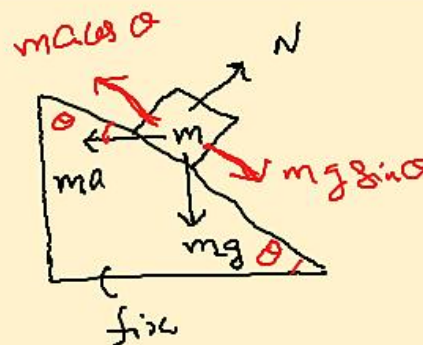
Let acc. of wedge be  $a$   
w.r.t. wedge

$$mg \sin \theta = ma \cos \theta$$

$$a = g \tan \theta$$

$$F = (M + m) a$$

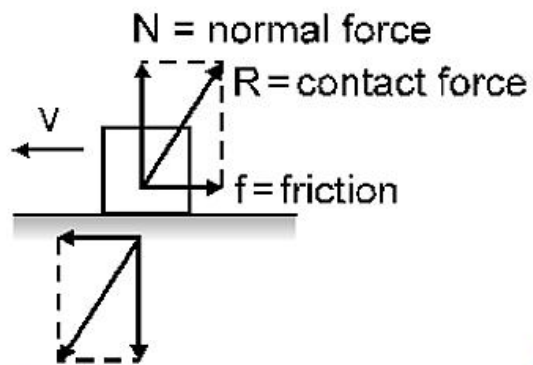
$$= (M + m) g \tan \theta$$





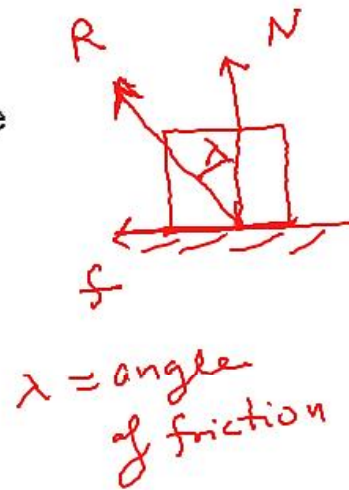
# FRICION

The component of contact force parallel to the surface is called friction (generally written as  $f$ ).



Net contact force is

$$R = \sqrt{f^2 + N^2}$$



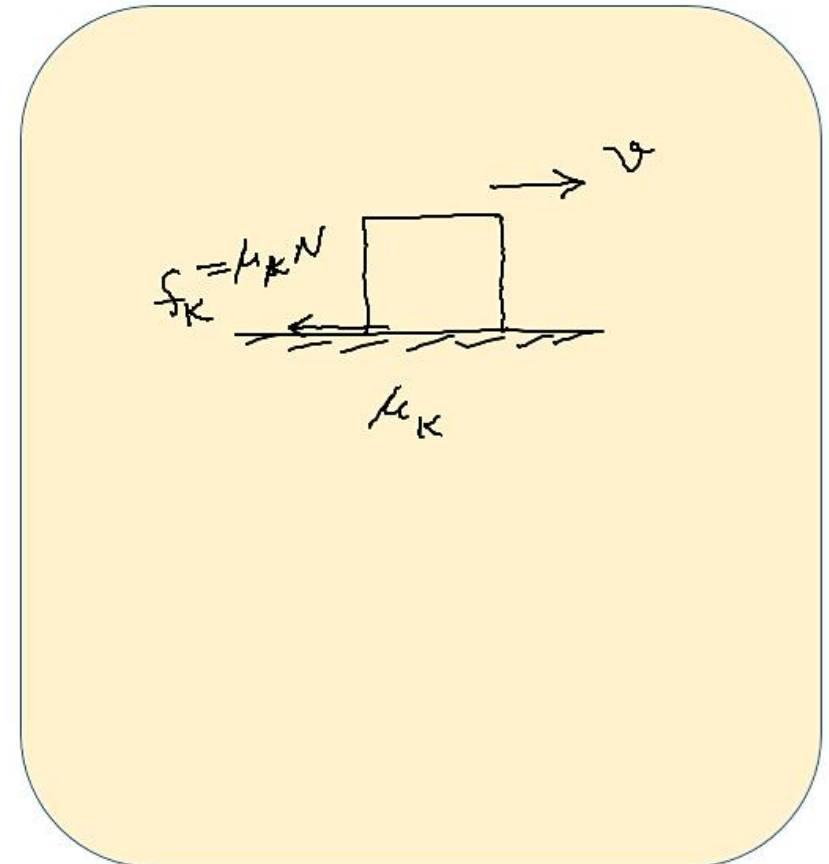
# Kinetic Friction

It exists due to relative motion between surfaces in contact and opposes the relative motion.

## Magnitude of Kinetic Friction

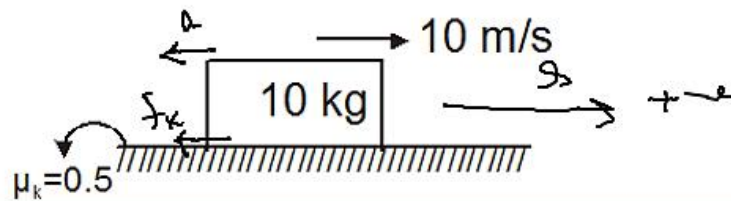
$$f_k = \mu_k N$$

$\mu_k$  is called the coefficient of kinetic friction



## Example

Find out the distance travelled by the blocks shown in the figure before it stops.



$$N = mg = 100$$

$$f_k = \mu_k N = 0.5 \times 100 = 50$$

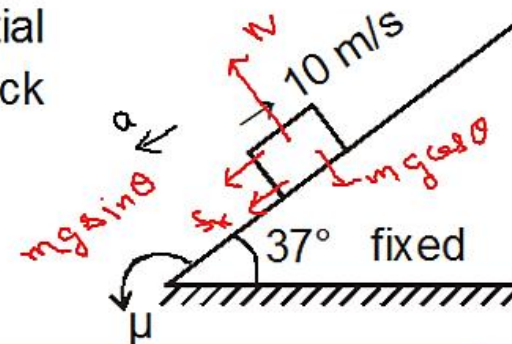
$$a = \frac{f_k}{m} = \frac{50}{10} = 5 \text{ m/s}^2 = a \rightarrow$$

$$v^2 = u^2 + 2as$$

$$0 = 100 + 2(-5)s \Rightarrow s = 10 \text{ m}$$

## Example

Find out the distance travelled by the block on incline before it stops. Initial velocity of the block is 10 m/s and coefficient of friction between the block and incline is  $\mu = 0.5$ .



$$f_k = \mu mg \cos \theta$$

$$a = \frac{mg \sin \theta + \mu mg \cos \theta}{m} = \frac{10 \times \frac{3}{5} + \frac{1}{2} \times 10 \times \frac{4}{5}}{1} = 10 \text{ m/s}^2$$

$$v^2 = u^2 + 2as \Rightarrow 0 = 100 - 2 \times 10 \times s$$

$$\Rightarrow s = 5 \text{ m}$$



# Static Friction

It exists between the two surfaces when there is tendency of relative motion but no relative motion along the two contact surface.

## Magnitude of Static Friction

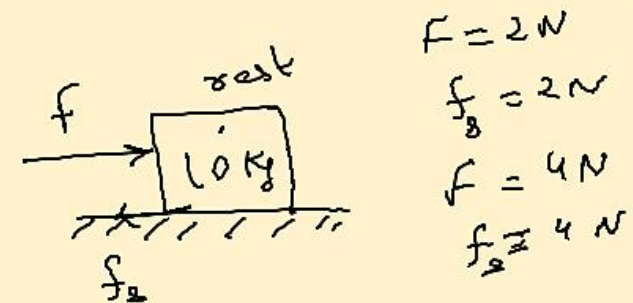
$$f_{\max} = \mu_s N$$

$\mu_s$  is called the coefficient of static friction

$$0 \leq f_s \leq f_{\max}$$

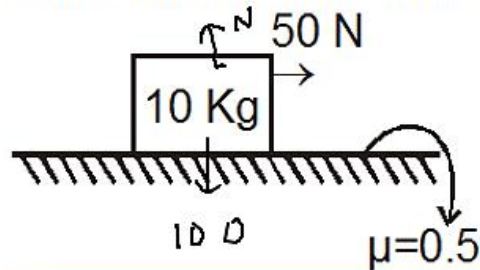
In general,

$$\mu_s > \mu_k$$



## Example

Find acceleration of block and friction force acting on the block. Initially the block is at rest.



$$g = 10 \text{ m/s}^2$$

$$N = 100$$

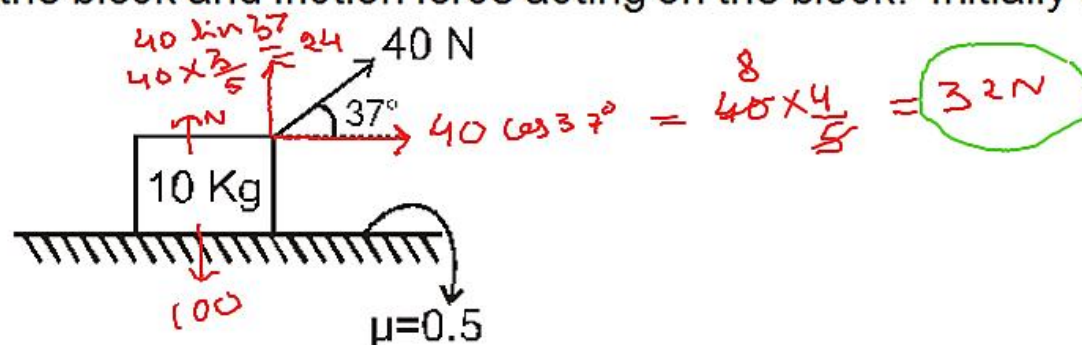
$$f_{\text{max}} = \mu N = 0.5 \times 100 = 50 \text{ N}$$

$$f = 50 \text{ N}$$

$$a = 0$$

## Example

Find out acceleration of the block and friction force acting on the block. Initially the block is at rest.



$$\begin{aligned}
 N + 24 - 100 &= 0 \Rightarrow N = 76 \\
 f_{\max} &= \mu N = \frac{1}{2} \times 76 = 38 \text{ N} \\
 a &= 0 \\
 f &= 32 \text{ N}
 \end{aligned}$$